A Soft-switched isolated Single Stage Bidirectional Three phase AC-DC Converter

Dibakar Das
Department of Electrical Engineering
Indian Institute of Science
Bangalore, India
dibakard@iisc.ac.in

Kaushik Basu
Department of Electrical Engineering
Indian Institute of Science
Bangalore, India
kbasu@iisc.ac.in

Abstract—The battery chargers in electric vehicles need to have high efficiency and power density. Moreover, bidirectional power flow capability is necessary for vehicle to grid (V2G) applications. This paper proposes a bidirectional isolated three phase AC-DC converter based on the dual active bridge (DAB) conversion principle and line frequency unfolding resulting in low switching loss. Sections of the fundamental components of line currents are generated using DAB modulation and then appropriately combined to produce the actual line currents. The proposed solution can be used for bidirectional power flow and power factor correction. The high efficiency due to reduced switching loss and improved power density makes it a promising solution for battery chargers particularly in vehicle to grid (V2G) applications.

Index Terms—Dual Active Bridge, Line frequency unfolding

I. INTRODUCTION

Rapidly depleting fossil fuels and the global warming concerns have increased the thrust towards electric vehicle (EV) technologies. Power electronic converters are necessary for interfacing the battery driven electric vehicles to a charging station or the utility grid. On board charging systems should be highly efficient and lightweight so that they do not increase the vehicle weight significantly. Moreover, in vehicle to grid (V2G) applications the converters should have bidirectional power flow capability.

Conventional EV chargers utilize two conversion stages for AC to DC power conversion [1]. The front end is an active hard-switched pulse width modulated (PWM) rectifier which is followed by a DC-DC converter for isolation and voltage matching. The intermediate DC link usually consists of a large and bulky electrolytic capacitor which increases the weight and reduces system reliability. To avert these issues, several works in the literature with single power conversion stage have been reported [2]–[4].

A single stage PWM unidirectional DC-AC converter using line frequency unfolding principle is discussed in [5]. The converter uses a phase shifted full bridge conversion strategy followed by line frequency unfolding. A similar idea based on resonant conversion principle utilizing dual bridge SRC modules is reported in [6]. The topology uses capacitor on the input of the line frequency unfold to filter the switching ripple components. However, use of series resonant converters results in high losses at light load conditions.

Dual active bridge converters were originally proposed in [7]. Dual active bridge converters offer a promising solution for high power DC-DC converters because of soft switching and bidirectional power flow capability [8]. Several single stage converter solutions have been proposed using the DAB principle. A three phase AC-DC using matrix converter on AC side and H-bridge on DC side is reported in [9]. The converter proposes a modulation strategy which enables soft switching of AC and DC bridges. The proposed modulation strategy results low frequency harmonics in line currents. Moreover, the detailed analysis on soft switching is not provided. A modulation strategy for obtaining open-loop power factor correction and no low frequency current harmonics with the topology in [9] is discussed in [10]. A modulation utilizing push-pull structure on AC side matrix converter and three phase VSI on DC side is reported in [11]. The AC side converter is high frequency switched which results in losses and low efficiency. A modulation strategy utilizing the topology in [9] which achieves primary bridge soft switching is reported in [12]. However, primary bridge zero current switching cannot be guaranteed to be completely lossless.

This paper proposes a novel three phase AC-DC converter topology along with a modulation strategy based on DAB principle. The proposed converter utilizes a line frequency unfolding scheme [6]. The modulation strategy results in soft-switching and line frequency unfolding leads to low switching losses. Moreover, the proposed converter offers a galvanically isolated single stage conversion with bidirectional power flow capability and controllable power factor. Analysis reveals that the DC side H-bridge of the converter is able to achieve soft switching for the entire line cycle which leads to improvement of efficiency. High efficiency and power density of the converter makes it a suitable candidate for on board electric vehicle chargers.

II. ANALYSIS OF THE PROPOSED CONVERTER

This section describes the proposed converter, modulation strategy and the derivation of important quantities of interest. The proposed converter topology is shown in Fig.1. On the DC side, the H-bridge converter is connected in parallel with primary windings of two high frequency transformer of turns ratio $1 : n$. The inductors $L_1$ and $L_2$ are responsible for the
The magnetizing inductance and losses in the system are not considered and all the switches are considered ideal for the simplicity of the converter analysis.

A. Unfolder Modulation

Consider the utility line to neutral voltages defined as,

\[ v_{an}(t) = V_p \cos(\theta) \]  
\[ v_{bn}(t) = V_p \cos\left(\theta - \frac{2\pi}{3}\right) \]  
\[ v_{cn}(t) = V_p \cos\left(\theta + \frac{2\pi}{3}\right) \]

\( V_p \) is the peak value of line to neutral voltage, \( \theta = \omega t = 2\pi ft \), where \( f \) is the line frequency. The line frequency unfolder is switched six times in a line cycle with the switching sequence shown in Fig. 2. The letters in the brackets indicate the connection of the three utility phases \((a, b \text{ and } c)\) to the terminals \(uv\) and \(vw\) respectively. The modulation of the

\begin{table}[h]
\centering
\begin{tabular}{cccccccc}
\hline
\textbf{Parameter} & \textbf{Value} & \\
\hline
\textbf{P} & 2.1 kW & \\
\textbf{L} & 270\mu H & \\
\textbf{n} & 0.67 & \\
\textbf{V_p} & 127V & \\
\textbf{V_0} & 400V & \\
\textbf{f} & 50Hz & \\
\textbf{f_s} & 20kHz & \\
\textbf{Power Factor} & 1.00 & \\
\hline
\end{tabular}
\caption{Design Parameters of the Converter}
\end{table}
TABLE II
UNFOLDER VOLTAGES IN VARIOUS SECTORS

<table>
<thead>
<tr>
<th>$\theta$</th>
<th>$\left(-\frac{2\pi}{3}, -\frac{\pi}{3}\right)$</th>
<th>$\left(-\frac{\pi}{3}, 0\right)$</th>
<th>$\left[0, \frac{\pi}{3}\right)$</th>
<th>$\left[\frac{\pi}{3}, \frac{2\pi}{3}\right)$</th>
<th>$\left[\frac{2\pi}{3}, \pi\right)$</th>
<th>$[\pi, \frac{4\pi}{3}]$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$v_{uw}$</td>
<td>$v_{ca}$</td>
<td>$v_{ac}$</td>
<td>$v_{ab}$</td>
<td>$v_{na}$</td>
<td>$v_{bc}$</td>
<td>$v_{cb}$</td>
</tr>
<tr>
<td>$v_{uv}$</td>
<td>$v_{ab}$</td>
<td>$v_{cb}$</td>
<td>$v_{bc}$</td>
<td>$v_{ac}$</td>
<td>$v_{ca}$</td>
<td>$v_{ha}$</td>
</tr>
</tbody>
</table>

Unfolder results in pulsating voltages $v_{uw}$ and $v_{uv}$ with peak value $\sqrt{3}V_p/2$. The voltage $v_{uw}$ lags the $v_{uv}$ by $\pi/3$ radians. For example, during $\theta \in \left[0, \frac{\pi}{3}\right]$ $S_{au}$, $S_{bu}$, $S_{cu}$ are ON. Thus, $v_{uw} = v_{ub}$ and $v_{uv} = v_{bc}$.

Accordingly, the operation principle of H bridges 2 and 3 are similar since the input to both the bridges is a pulsating DC voltage with a phase shift. Moreover, the analysis over $\theta \in \left[-\frac{2\pi}{3}, -\frac{\pi}{3}\right]$ is sufficient owing to the periodicity of the waveforms. Consider the sector $\theta \in \left[-\frac{\pi}{3}, \frac{\pi}{3}\right]$ in Fig.2. The switching functions result in a voltage,

$$v_{uw} = \begin{cases} v_{ac} & -\pi/3 \leq \theta < 0 \\ v_{cb} & 0 \leq \theta < \pi/3 \end{cases}$$

$$v_{uv} = \begin{cases} v_{ab} & -\pi/3 < \theta \leq 0 \\ v_{bc} & 0 \leq \theta < \pi/3 \end{cases}$$

The voltages in other sectors can be similarly identified and is shown in Table II. It can be seen from Fig.2 that $u$ is always connected to the most positive line-neutral voltage and $w$ is always connected to the most negative line-neutral voltage. Thus each of the switches in these legs ($S_{ja}$ and $S_{jw}$, $j \in \{a, b, c\}$) only need to block unipolar voltage and are switched every $\frac{2\pi}{3}$ radians. However, the switches of the middle leg are switched every $\frac{\pi}{3}$ radians and need to block bidirectional voltage. All the switches need to carry bidirectional current. Thus, a T-type multilevel structure is used for the line frequency unfolder as shown in Fig.1.

**B. Modulation of DAB units**

The proposed converter enables bidirectional power transfer at any power factor. However, for illustration of the dual active bridge modulation in Fig.2, vehicle to grid (DC to AC) power transfer at unity power factor is considered. In general, the reference currents $i_u$, $i_b$ and $i_c$ (see Fig.1) are given by,

$$i_u(t) = I_p \cos(\omega t + \phi)$$

$$i_b(t) = I_p \cos\left(\omega t + \phi - \frac{2\pi}{3}\right)$$

$$i_c(t) = I_p \cos\left(\omega t + \phi + \frac{2\pi}{3}\right)$$

$I_p$ is the peak of line current and $\phi$ is the power factor angle. Since the unfolder output waveforms are periodic after every $\frac{2\pi}{3}$, $\theta \in \left[-\frac{2\pi}{3}, \frac{\pi}{3}\right]$ is analysed henceforth. During this period, phase $a$ is connected to $u$ and thus the reference current $i_u = i_a$.

Conventional phase shift modulation is used for synthesizing the currents $i_u$ and $i_w$. Accordingly, the primary and secondary H-bridges are modulated to produce a square waveform with 50% duty ratio as shown in Fig.3a. A phase shift is given between these waves to carry out the power transfer. For the DAB converter with phase shift square wave modulation with frequency $f_s$ as shown in Fig.3a, the voltages applied across the inductor $L$ are given by,

$$v_L = \begin{cases} V_1 + \frac{V_2}{n} & ; 0 \leq t < \Delta t \\ V_1 - \frac{V_2}{n} & ; \Delta t \leq t < \frac{T}{2} \\ -V_1 - \frac{V_2}{n} & ; \frac{T}{2} \leq t < \frac{T}{2} + \Delta t \\ -V_1 + \frac{V_2}{n} & ; \frac{T}{2} + \Delta t \leq t < T_s \end{cases}$$

(9)

The inductor current is derived using the following expression,

$$L \frac{di_L}{dt} = v_L(t)$$

(10)

Noting that the current waveform has half wave symmetry $i_L(0) = -i_L(T_s/2)$. The currents $I_1$ and $I_2$ are given by,

$$I_1 = \frac{-1}{4nL_f} \left(V_2\delta - V_2 + nV_1\right)$$

(11)

$$I_2 = \frac{1}{4nL_f} \left(V_2 - nV_1 + n\delta V_1\right)$$

(12)

The power transferred from port 1 to 2 is,

$$P_{12} = \frac{V_1 V_2}{8nL_f} \delta (2 - \delta)$$

(13)

where $\Delta t = \delta T_s/4$. Considering the DAB operation between H bridges 1 and 2, $V_1 = V_o$, $V_2 = v_{uw}$. Moreover, the average power at the $uw$ terminal is $P = v_{uw} \times i_u$. Thus, the current waveform $i_u$ is given by,

$$i_u(\theta) = \frac{V_o}{8nL_f} \delta (2 - \delta)$$

(14)

The current waveform $i_u$ is shaped by varying the phase shift between H bridges 1 and 2, $\delta_{12}$, over line cycle as shown in Fig.3. The expression of $\delta_{12}$ can be derived from (14) as,

$$\delta_{12}(\theta) = 1 - \sqrt{1 - \frac{8nL_f \delta v_u(\theta)}{V_o}}$$

(15)

For $\theta \in \left[-\frac{2\pi}{3}, \frac{\pi}{3}\right]$, $\hat{i}_u = \hat{i}_a = I_p \cos(\omega t + \phi)$. For unity power factor operation, the variation of $\delta_{12}$ is shown. The phase shift $\delta_{13}$ between bridges 1 & 3 can be similarly derived from the reference current $-i_w$.

$$\delta_{13}(\theta) = 1 - \sqrt{1 + \frac{8nL_f \delta v_w(\theta)}{V_o}}$$

(16)

**C. Soft Switching features**

Consider the DAB converter operating with conventional phase shift modulation scheme as discussed in the previous section. The switching transition at $t = 0$ is considered to demonstrate capacitor assisted soft switching in Fig.4. The converter is going from negative active state ($S_2$ and $S_3$ ON) to
Fig. 3. Waveforms illustrating DAB operation (a) DAB formed by H-bridges 1 and 2 and operating waveforms (b) Operating waveforms for DAB formed by H-bridges 1 and 2 and DAB formed by H-bridges 1 and 3

Fig. 4. Capacitor assisted soft turn-off and turn-on

...the positive active state ($S_1$ and $S_4$ ON). Accordingly, switch $S_2$ is turned OFF and $S_1$ is turned on after dead time as shown in Fig.4. Assuming that the current at the instant of turn-off of $S_2$ to be less than zero, the switch $S_2$ is conducting prior to its turn-off. This implies $v_{C_2} = 0$ (Fig.4a). When switch $S_2$ is turned off, the current quickly shifts to the capacitors $C_1$ and $C_2$ (Fig.4b) and the switch channel is turned off before the voltage across the capacitor can build up implying ZVS. The inductor current discharges the capacitor $C_1$ and the diode starts conducting once the voltage $v_{C_1} = 0$. The switch $S_1$ is turned on when its body diode is conducting thus resulting in ZVS turn on.

Thus, the current polarity $I_1$ should be negative to facilitate capacitor assisted soft switching. Similarly, analysing the switching transient at $t = \Delta t$, $I_2$ should be greater than zero to facilitate soft switching.

For power factor less than $30^\circ$, the reference current waveforms $i_u$ and $-i_w$ are always positive. This means $\delta_{12}$ and $\delta_{13}$ are always positive and bridge 2 and 3 square waveforms are phase shifted with respect to bridge 1 square waveform. When the Bridge 1 switches at $t = 0$, the sum of bridge 2 and bridge 3 currents needs to be switched.

For the converter operation with the design parameters listed in Table I, the current $I_p = 11.4A$. Accordingly, the values $\delta_{12}$ and $\delta_{13}$ can be determined using (15) and (16) respectively. The currents at the instants $t = 0$, $\Delta t_{12} = \delta_{12}T_s/4$ and $\Delta t_{13} = \delta_{13}T_s/4$ can be determined for every switching cycle using (11) and (12). Fig.5 shows the current magnitudes at the instant of bridge 1, 2 and 3 switching. Since the waveforms are periodic after every $\pi/3$, only $\theta \in (-\pi/3, \pi/3)$ is shown. For the leading bridge (H-bridge 1 in the present scenario) to be
soft switched, the current at the switching instant \( t = 0 \) should be negative. It can be seen from Fig.5a that, H-bridge-1 always switches at \( t = 0 \) with negative current. This implies that the primary side H-bridge is soft switched over the entire line cycle. ZVS happens in Bridges 2 and 3 when the current during switching at \( t = \Delta t \) is positive. Bridge 2 current is positive only during \( \theta \in (-\theta_2, \frac{\pi}{3} - \theta_2) \) Thus ZVS happens only in the aforesaid region which repeats after every \( \pi/3 \). Similarly Bridge 3 is soft switched for \( \theta \in (-\frac{\pi}{3}, -\theta_1) \cup (\frac{\pi}{3} - \theta_1, \frac{\pi}{3}) \). Thus partial ZVS happens for AC side H-bridges in certain sections of the line cycle.

### III. SIMULATION AND EXPERIMENTAL RESULTS

The proposed converter topology and modulation strategy was simulated in MATLAB with the parameters described in Table I and DC to AC power flow.

Fig.6a shows the operating waveforms for a switching cycle for the DAB unit formed by H bridges 1 and 2. It can be seen that the inductor current varies linearly according to the voltages \( v_p \) and \( v_{uv} \). Similar behaviour is observed for the DAB unit formed by H bridges 1 and 3 (Fig.6b). Fig.7c shows the operation of the primary H-bridge at a given instant in the line cycle (\( \theta = \pi/18 \)). The different current slopes
indicate that both the DAB units are performing with non-identical phase shifts as desired. Fig.6d shows the phase A line to neutral voltage along with the three phase currents. The currents are balanced and \( i_a \) is in phase with \( v_{an} \) confirming UPF operation. The system was simulated at a power level of 2.1 kW which corresponds to a line current peak of 11.3 A. This can be verified from Fig.6d. The experimental switching cycle waveforms for the dual active bridge units are shown in Fig.7b and c. The primary voltage and the secondary currents for a given switching instant are shown in Fig.7d. The sum of the transformer currents \( i_1' \) and \( i_2' \) calculated using math operation is shown in red. This sum has exact resemblance to \( i_L \) and is scaled by turns ratio \( n \).

IV. Conclusion

This paper presented a novel single stage converter topology and modulation that can enable bidirectional power flow. Use of line frequency unfolding scheme enables low switching losses. Use of DAB conversion technique reduces the switching losses through soft switching. It is observed that use of the proposed modulation strategy results in the primary side H-bridge to be completely soft-switched. However, secondary side H-bridges working with pulsating DC voltages are partially soft switched in certain sections of the line cycle.

REFERENCES


